ALTERNATIVE A
COURSE CODE: COURSE TITLE:
CREDIT UNIT
TIME ALLOWED
INSTRUCTION:

## PHY314

Numerical Computation
2
(2 HRS)
Answer question 1(section A) and any other three questions in section B

## SECTION A

## Question 1 (25marks)

(i) Round the following numbers to 4 significant numbers (a) 12.0234 ( $1 / 2 \mathrm{mks}$ ) (b) 529.501( $1 / 2 \mathrm{mks}$ )
(ii) Transform the equation, $T=2 \pi \sqrt{\frac{l}{g}}$ into a straight line equation ( 2 mks )
(iii) Using the method of least squares on the table below, calculate the (a) slope (2mks) and (b) intercept ( 2 mks ) (c) relationship between the variables. ( $21 / 2 \mathrm{mks}$ )

| t | 5 | 12 | 19 | 26 | 33 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| x | 25 | 28 | 32 | 38 | 41 |

(iv) What is the augmented matrix of the following equations?

$$
\begin{aligned}
& 2 x+y-z=5 \\
& x+3 y+2 z=5 \\
& 3 x-2 y-4 z=3(1 \mathrm{mks})
\end{aligned}
$$

(v) Solve the system of linear equations using Gaussian elimination method ( 4 mks )
(vi) Write the forward difference table for the function, $f(x)=x^{2}+2 x+3$ at $\mathrm{x}=0,1, \ldots 6$. (3mks)
(vii) Integrate the following function, $f(x)=3 x^{2}+5 x-1$ of x with respect to using Trapezoidal rule ( 4 mks ).
(viii) List the different methods of solving first order ordinary differential equations ( 2 mks ).
(ix) What are the merits of Bisection method? (1mk)
(x) Given the augmented matrix, $\left[\begin{array}{cccc}25 & 1 & -1 & 28 \\ 1 & 30 & 2 & 59 \\ 3 & -2 & -20 & 19\end{array}\right](11 / 2 \mathrm{mks})$

## SECTION B

## Question 2

(a) Round the following numbers to 4 significant numbers (i) 1.412519 (ii) 6.324319 (iii) 3.162159.(6mks)
(b) A student measured the length of a stick whose actual length of 72.5 cm as 72.3 cm . What is the (i) absolute error in the measurement ( 4 mks ) (ii) Relative error of the measurement ( 2 mks ) (iii) percentage error of the measurement (3mks).

## Question 3

Given the equations

$$
\begin{aligned}
& 2 x+3 y=13 \\
& x-y=-1
\end{aligned}
$$

(i) Write down the augmented matrix ( 3 mks )
(ii) (ii) Use Gaussian elimination method to solve the problem (12mks).

## Question 4

Find the value of $y$ at $x=0.2$ if $y^{\prime}+2 y=0 ; y(0)=1$ step-length 0.2 using second-order RungaKutta formula ( 15 mks ).

## Question 5

Integrate the following function, $f(x)=3 x^{2}+5 x-1$ of x with respect to using Simpson's $\frac{1}{3} \mathrm{rd}$ rule ( 15 mks ).

