



NATIONAL OPEN UNIVERSITY OF NIGERIA
University Village, Plot 91, Cadastral Zone, Nnamdi Azikwe Express Way, Jabi-Abuja
FACULTY OF SCIENCES
Department of Mathematics
2021_2 Examinations...

Course Code: MTH307

Course Title: Numerical Analysis II

Credit Unit: 3

Time Allowed: 3 Hours

Total: 70 Marks

Instruction: Answer Question One (1) and Any Other 4 Questions

1. (a) State the properties of Chebyshev polynomials. **(5 marks)**
(b) Use Chebyshev interpolation to find a cubic polynomial approximation to $(1+x)^{\frac{1}{2}}$ over $[-1, 1]$. **(17 marks)**
2. (a) Distinguish between Initial Value Problem and Boundary Value Problem. **(5 marks)**
(b) Solve the Boundary Value Problem (BVP) $(1+x^2)y'' + 2xy' - y = x^2$ with the boundary conditions $y(0) = 1$ and $y(1) = 0$, using a step length of 0.25. **(7 marks)**
3. (a) State the properties of a cubic spline interpolation. **(5 marks)**
(b) Use Hermite cubic interpolation to estimate the value of $\sqrt{55}$ taking $f(x) = \sqrt{x}$, $x_1 = 49$, $x_2 = 64$. **(7 marks)**
4. (a) Enumerate the classification of least square approximation method and explain each.

(5 marks)

(b) Derive the least square formula for discrete data.

(7 marks)

5. (a) Distinguish between Hermite polynomial and cubic spline.

(5 marks)

(b) Find the cubic spline given the data below

x	0	2	4	6
y	1	9	41	41

where $M_0 = 0$ and $M_3 = -12$.

(7 marks)

6. (a) Define Simpson's $\frac{1}{3}$ rule.

(5 marks)

(b) Evaluate $\int_0^{\frac{\pi}{3}} \sin x dx$ with $h = \frac{\pi}{12}$, correct to 5 decimal places using Trapezoidal rule.

(7 marks)