## NATIONAL OPEN UNIVERSITY OF NIGERIA PLOT 91, CADASTRAL ZONE, NNAMDI AZIKIWE EXPRESSWAY, JABI - ABUJA FACULTY OF SCIENCES

#### DEPARTMENT OF PURE AND APPLIED SCIENCE

#### 2021\_2 EXAMINATIONS.co

<b>COURSE CODE:</b>	PHY311
<b>COURSE TITLE:</b>	KINETIC THEORY AND STATISTICAL MECHANICS
<b>CREDIT UNIT:</b>	2
TIME ALLOWED:	(2 HRS)

**INSTRUCTION:** Answer question 1 and any other three questions

## **QUESTION 1**

(a) Define the following terms; (i) Most probable velocity (ii) Root-mean-square velocity [5 marks]

(b) Show that the most probable speed at which n(v) has its maximum value  $V_P = \sqrt{\frac{2RT}{M}}$ [10marks]

(c) Show that the root mean square speed of gas molecule  $V_{rms} = \sqrt{\frac{3RT}{M}}$  [10marks]

## **QUESTION 2**

(a) Derive Dulong-petit's law on the basis of equipartition theorem [5marks]

(b) Show that for a perfect gas represented by a grand canonical ensemble, the probability of finding the subsystem with n atoms is given by Poisson distribution

 $\omega(n) = \frac{1}{n!} (n)^n e^{-\bar{n}}$  where  $\bar{n}$  is the number of atoms present [10marks]

## **QUESTION 3**

(a) If twelve particles are distributed randomly between two boxes A and B with equal probability, then calculate

- (i) The probability of the distribution (8, 4)
- (ii) The probability of the most probable distribution
- (iii) The probability of least probable distribution.

(b) Find the probability that in tossing a coin 12 times we get (i) 4 heads 8 tails (ii) 6 heads 6 tails [6marks]

## **QUESTION 4**

Three particles are to be distributed in four energy states *a*, *b*, *c* and *d* write down all the possible ways for such a distribution if the particles are (i) Fermions (ii) Bosons [15marks]

# **QUESTION 5**

Let  $v_x$ ,  $v_y$ ,  $v_z$  represent the three Cartesian components of velocity of a molecule in a gas. Using symmetry consideration and equipartion theorem, deduce, expression for the following mean values in terms of K, T and m. (i)  $\langle v_x \rangle$  (ii)  $\langle \bar{v}_x^2 \rangle$  (iii)  $\langle v_x v_z \rangle$  (iv)  $\langle (v_x + bv_y)^2 \rangle$ 

[15marks]