



NATIONAL OPEN UNIVERSITY OF NIGERIA
PLOT 91, CADASTRAL ZONE, NNAMDI AZIKIWE EXPRESSWAY, JABI, ABUJA
FACULTY OF SCIENCES
DEPARTMENT OF COMPUTER SCIENCE
OCTOBER, 2019 EXAMINATIONS

COURSE CODE: CIT342

COURSE TITLE: FORMAL LANGUAGES AND AUTOMATA THEORY

COURSE CREDIT: 3 UNITS

TIME ALLOWED: 2½ HOURS

INSTRUCTION: ANSWER QUESTION 1 AND ANY OTHER FOUR (4) QUESTIONS

- 1a) Distinguish between the strings and the words of a language (*2 marks*)
- b) Compare Non-Determinism to Determinism. Which of them is ideal for use in a computer system? (*4 marks*)
- c) Differentiate between Kleene Star Closure (*) and Plus (+) operations over the alphabet of a grammar. (*4 marks*)
- d) Explain any three (3) Applications of Finite Automata (*9 Marks*)
- e) Give regular expressions that generate each of the following languages. In all cases, the alphabet is $\Sigma = \{a, b\}$. (a).
- (i) The language $\{w \in \Sigma^* \mid |w| \text{ is odd}\}$. (*1 mark*)
- (ii) The language $\{w \in \Sigma^* \mid w \text{ has an odd number of a's}\}$. (*1 mark*)
- (iii) The language $\{w \mid w \text{ contains at least two a's, or exactly two b's}\}$ (*1 mark*)
- 2a) Using the Set language, define the following terms and concepts: (*9 marks*)
- (i) Union (ii) Intersection (iii) Set Concatenation (iv) Kleene-star,
(v) Set Subtraction (vi) Complement
- (b) State regular expressions that generate each of the following languages. In all cases, the alphabet is $\Sigma = \{a, b\}$. (a).
- i) The language $\{w \in \Sigma^* \mid w \text{ ends in a double letter}\}$. (*1 mark*)
- ii) The language $\{w \in \Sigma^* \mid w \text{ does not end in a double letter}\}$. (*1 mark*)
- iii) The language $\{w \in \Sigma^* \mid w \text{ contains exactly one double letter}\}$. (*1 mark*)

3a) Briefly explain the following:

(i) Turing-decidable language (3 marks)

(ii) Turing-recognizable language (2 marks)

b) State the characteristics of grammars in Greibach Normal Form (2 marks)

c) State the use(s) of Greibach Normal Form (2 marks)

d) Formally define Type 1 grammar (3 marks)

4a) Define context-sensitive grammars (2 marks)

b) What do you understand by decision problems? (3 marks)

c) What do you understand by the term automata theory? (2 marks)

d) Define leftmost and rightmost derivation of a grammar. State the distinction between the two. (5 marks)

5a) Consider the grammar: $G = (\{S, A, B, C\}, \{a, b, c\}, S, P)$

Where, $P = \{S \rightarrow ABC, A \rightarrow aA, A \rightarrow \lambda, B \rightarrow bB, B \rightarrow \lambda, C \rightarrow cC, C \rightarrow \lambda\}$, derive the string **abc** in a:

i) leftmost derivation (2 marks)

ii) rightmost derivation (2 marks)

b) Draw the derivation tree for the leftmost derivation in question (5a) above. (3½ marks)

c) When is a grammar said to be in **Chomsky normal form**? (4½ marks)

6a) Prove that context-free languages are closed under the formation of union. (6 marks)

b) In the context of automata theory, briefly describe the following terms:

i. Recognised language (2 marks)

ii. Run (2 marks)

iii. Transducer (2 marks)