

## NATIONAL OPEN UNIVERSITY OF NIGERIA University Village, Plot 91, Cadastral Zone, Nnamdi Azikwe Express Way, Jabi-Abuja

## FACULTY OF SCIENCES DEPARTMENT OFMATHEMATICS 2021\_1 Examinations ....

Course Code: MTH302

Course Title: Elementary Differential Equations II

Credit Unit: 3

Time Allowed: 3 Hours Total: 70 Marks

**Instruction:** Answer Question One (1) and Any Other 4 Questions

1. (a)Determine whether x = 0 is a regular singular point of the following differential equations

(i) 
$$2x^2y'' + 7x(x+1)y' - 3y = 0$$

(3 marks)

(ii) 
$$x^3y'' + 2x^2y' + y = 0$$

(3 marks)

(b) Use the power series method to find the general solution near x = 0 of

$$y'' + y = 0.$$
 (16 marks)

- 2. Find the first four terms in each portion of the series solution around  $x_0 = 0$  for the following differential equation  $(x^2 + 1)y'' 4xy' + 6y = 0$  (12 marks)
- 3. Find the eigenvalues and eigenfunctions of

$$y'' - 4\lambda y' + 4\lambda^2 y = 0; y'(1) = 0, y(2) + 2y'(2) = 0$$
 (12 marks)

4. Verify the orthogonality property for the Sturm-Liouville problem

$$y'' + \lambda y = 0$$
;  $y'(0) = 0$ ,  $y(\pi) = 0$  if the problem has the eigenvalues

$$\lambda_n = \left(n - \frac{1}{2}\right)^2$$
 corresponding to the eigenfunctions

$$y_n(x) = A_n \cos\left(n - \frac{1}{2}\right) x$$
,  $n = 1, 2, ...$  (12 marks)

- 5. Find a Fourier cosine series for f(x) = x on (0, 3). (12 marks)
- 6. Find a Fourier cosine series for  $f(x) = e^x$  on  $(0, \pi)$ . (12 marks)